

On the speed-accuracy trade-off and speed-curvature power law of tongue movements in repetitive speech

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Gefördert durch
DFG Deutsche
Forschungsgemeinschaft



LabPhon16, June 19–22, 2018, Lisboa, Portugal

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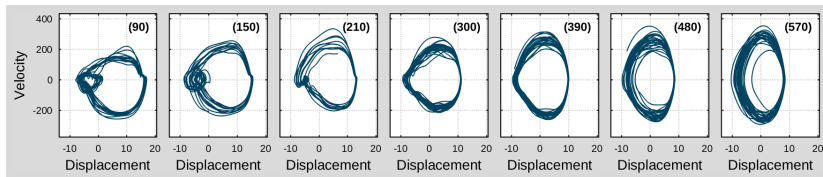
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- specifically: sequences of **[tatata...]** and **[kakaka...]**
- about 4000 syllables of [ta] and [ka] each
- six native speakers of **German and English**

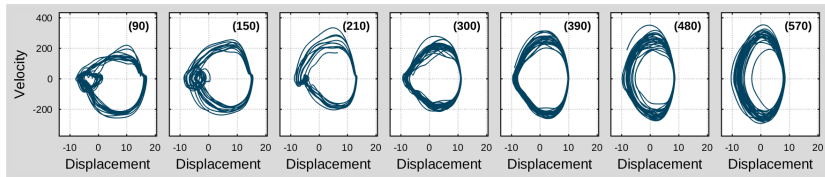
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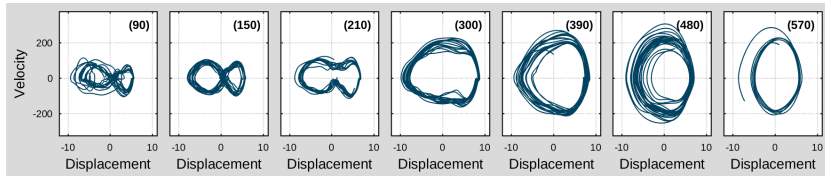


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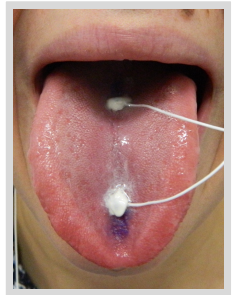


- **non-speech** (trumpet double tonguing):



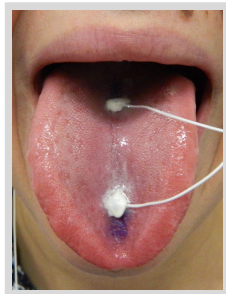
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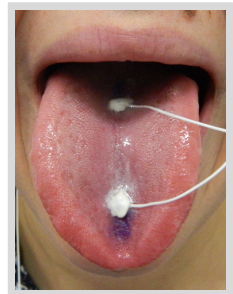
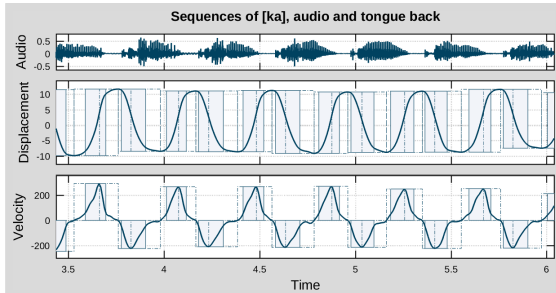
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- **segmentation of continuous motion** by zero velocity criterion



Kinematic relations

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- **standard model of speech gestures** (linear oscillator with critical damping, Fowler et al., 1980; Browman and Goldstein, 1986; Saltzman and Munhall, 1989)

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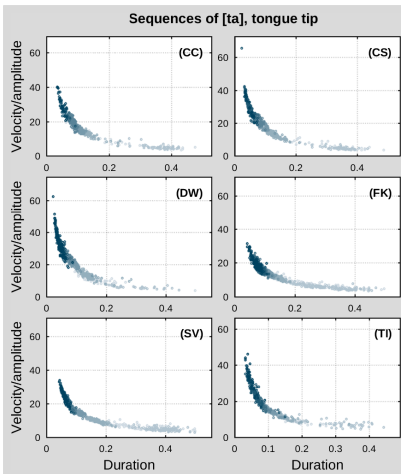
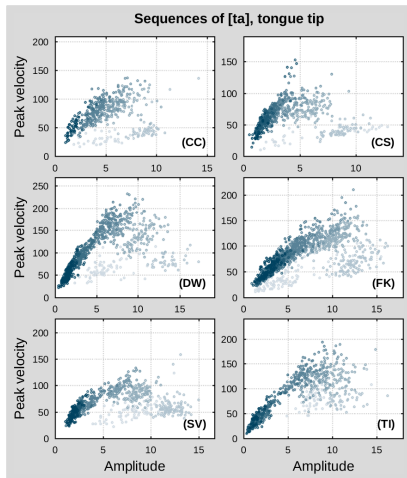
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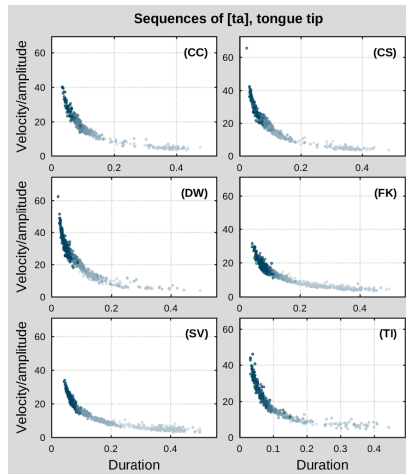
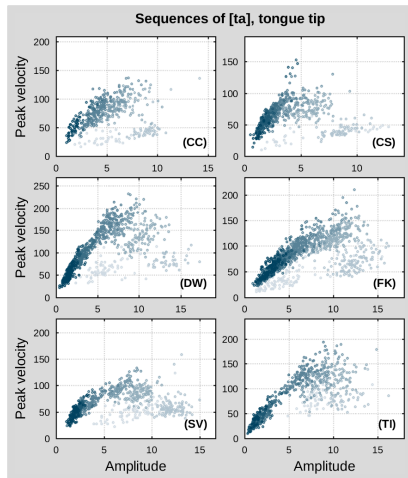
- **direct proportionality** of peak velocity v^* and amplitude A
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- **empirical evidence** repeatedly reported, e.g., in Ostry et al. (1983), Munhall et al. (1985), and Vatikiotis-Bateson and Kelso (1990)

Kinematic relations



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- divergence of $A-v^*$ correlation at **larger amplitudes** (slower rates) considered in [Sorensen and Gafos \(2016\)](#)

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- **velocity gain factor** k segregates geometrical subunits
- **exponent** β is consistently found to be close to the value of $1/3$

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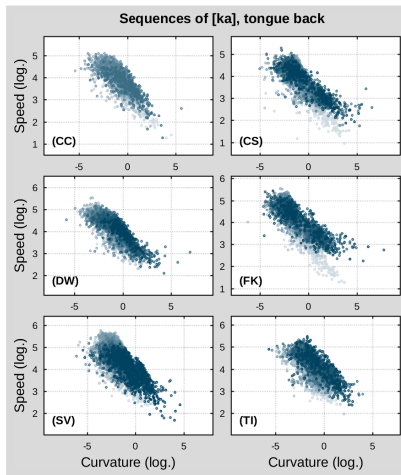
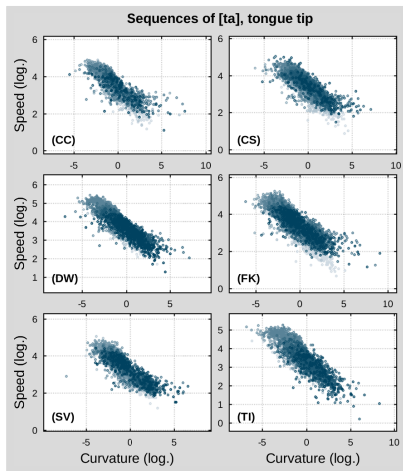
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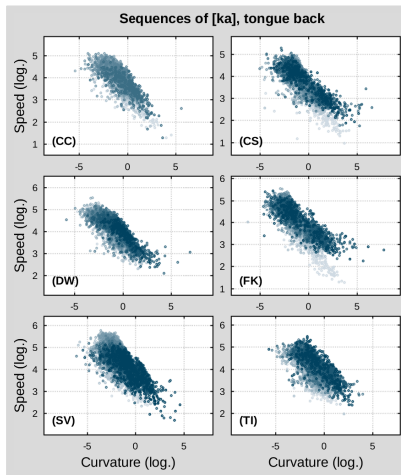
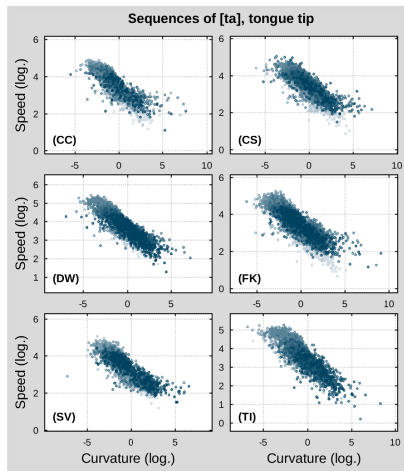
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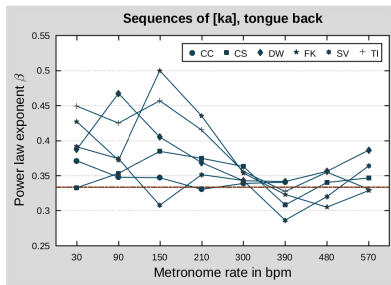
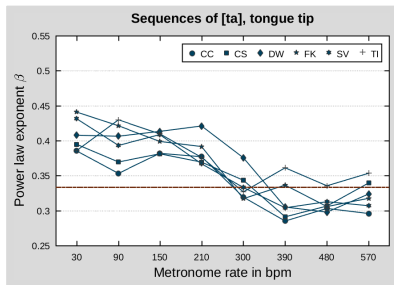
- clear evidence for the **power law** in speech

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- new: significant **rate dependency** of the power law exponent β



- closest match with commonly found value of $1/3$ at metronome rate of 300 bpm (**fast speech rate**)

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Why an exponent of $1/3$?

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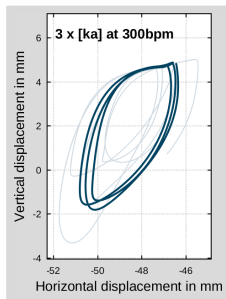
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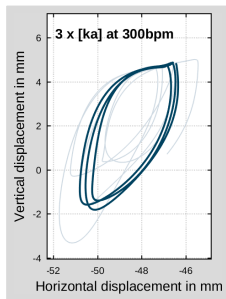
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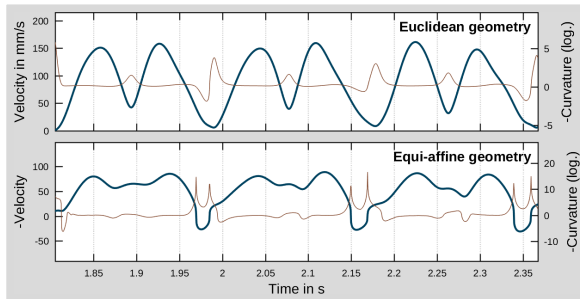
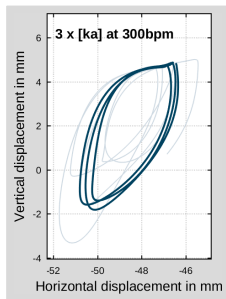


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How to achieve this in speech?

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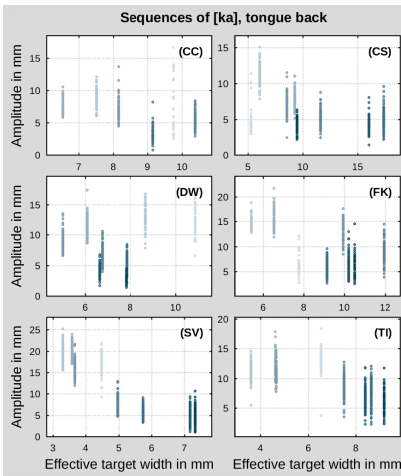
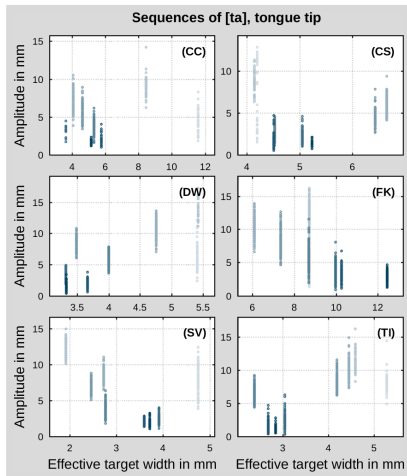
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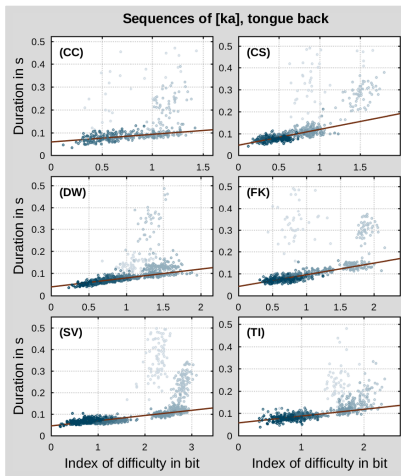
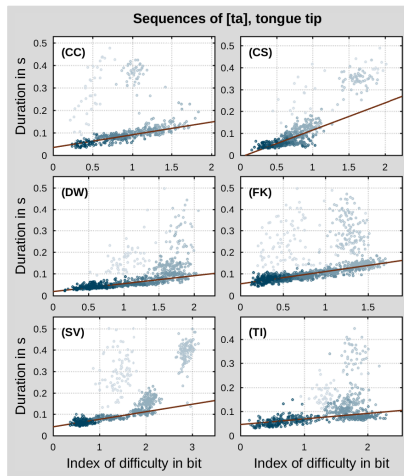
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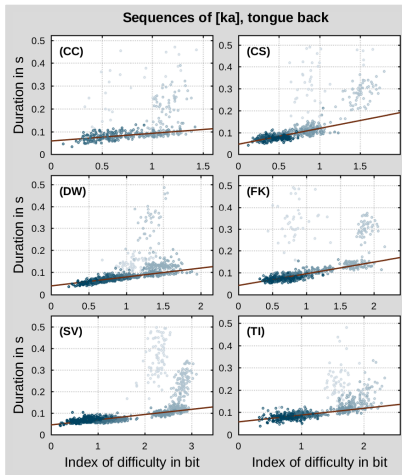
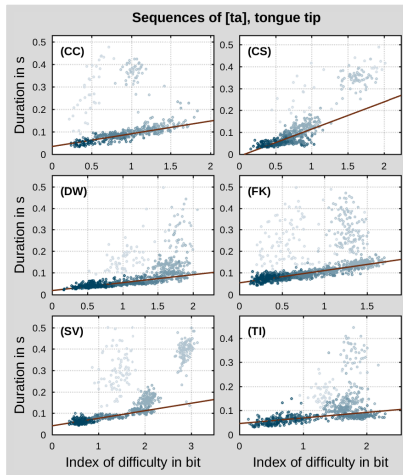
- observations of **movement duration** T should reveal the **linearity of Fitts' law**

$$T = a + b ID \quad (8)$$

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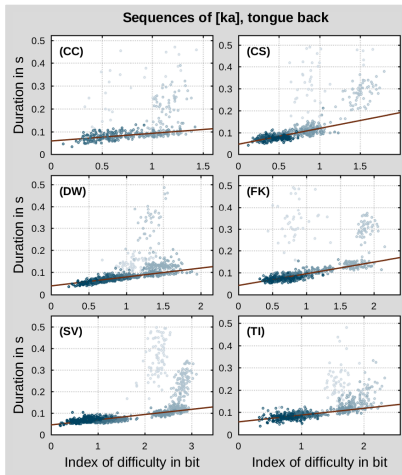
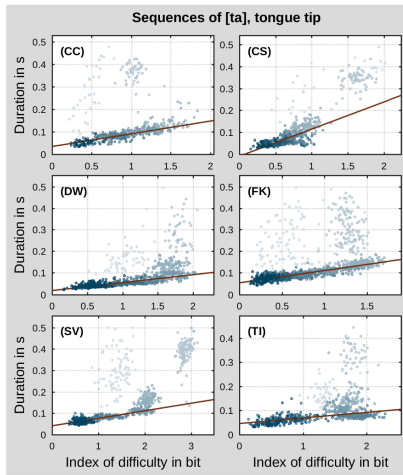


Fitts' law



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- **fast rates** (≥ 150 –210 bpm, dark shades) abide to Fitts' law
- **slowest rates** (< 150 –210 bpm, bright shades) do not

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- other models with different dynamics exist but have not been investigated yet (Kröger et al., 1995; Sorensen and Gafos, 2016)

References

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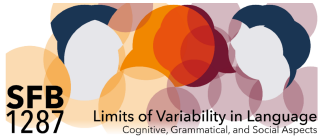
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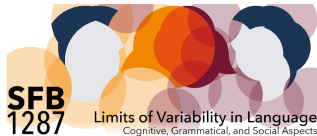
Thank you very much.



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Support from DFG SFB 1287 and ERC AdG 249440 is gratefully acknowledged.



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