

*King's College London*

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# Assigning Likelihoods to Interlocutors' Beliefs and Arguments

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## Structured argumentation based on ASPIC+: Preliminaries

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- ❖ Argumentation Theory  $AT = \langle AS, K \rangle$
- ❖ Argumentation System  $AS = \langle L, R, \text{---}, n \rangle$ 
  - ❖  $L$                       Language
  - ❖  $R = R^s \cup R^d$       Strict/Defeasible inference rules
  - ❖  $\text{---}$                       Generalised negation
  - ❖  $n : R^d \rightarrow L$       Name for defeasible rules
- ❖ Knowledge-base  $K = K^n \cup K^p$  Axiom and ordinary premises

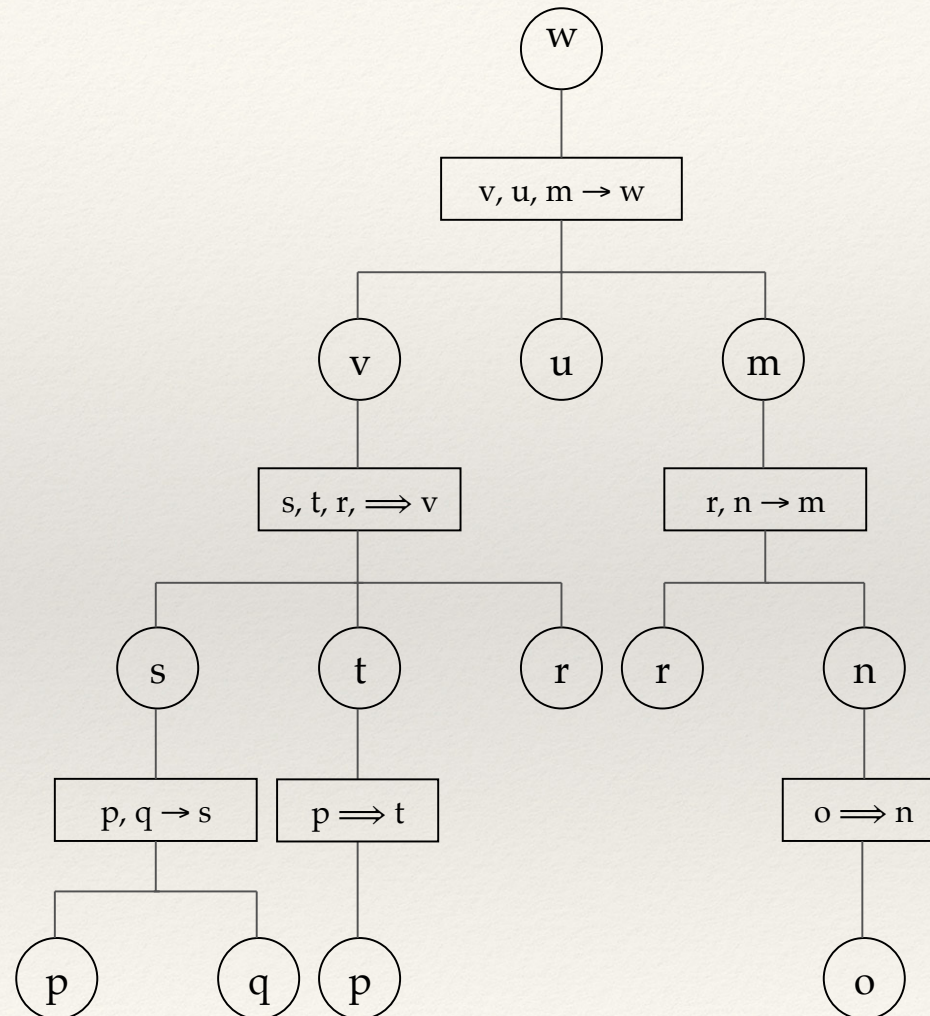


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# Structured argumentation based on ASPIC+:

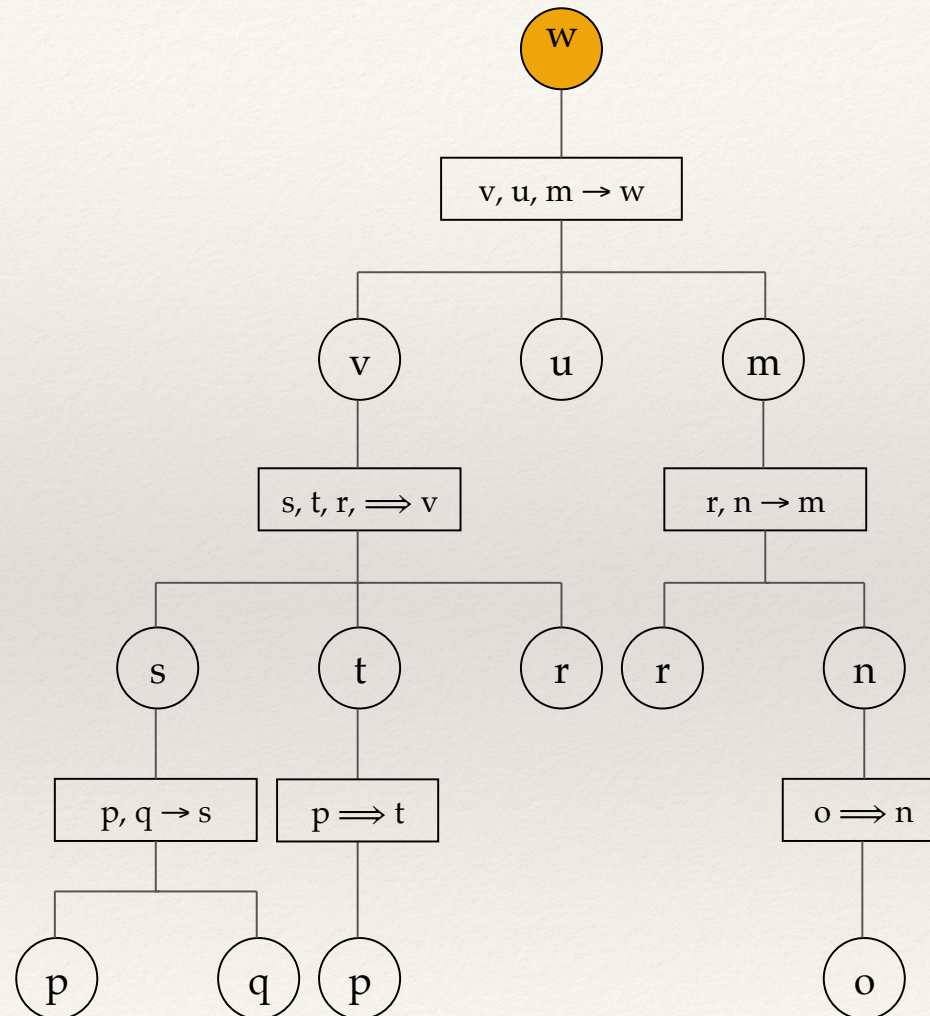
## Arguments

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# Structured argumentation based on ASPIC+: Arguments

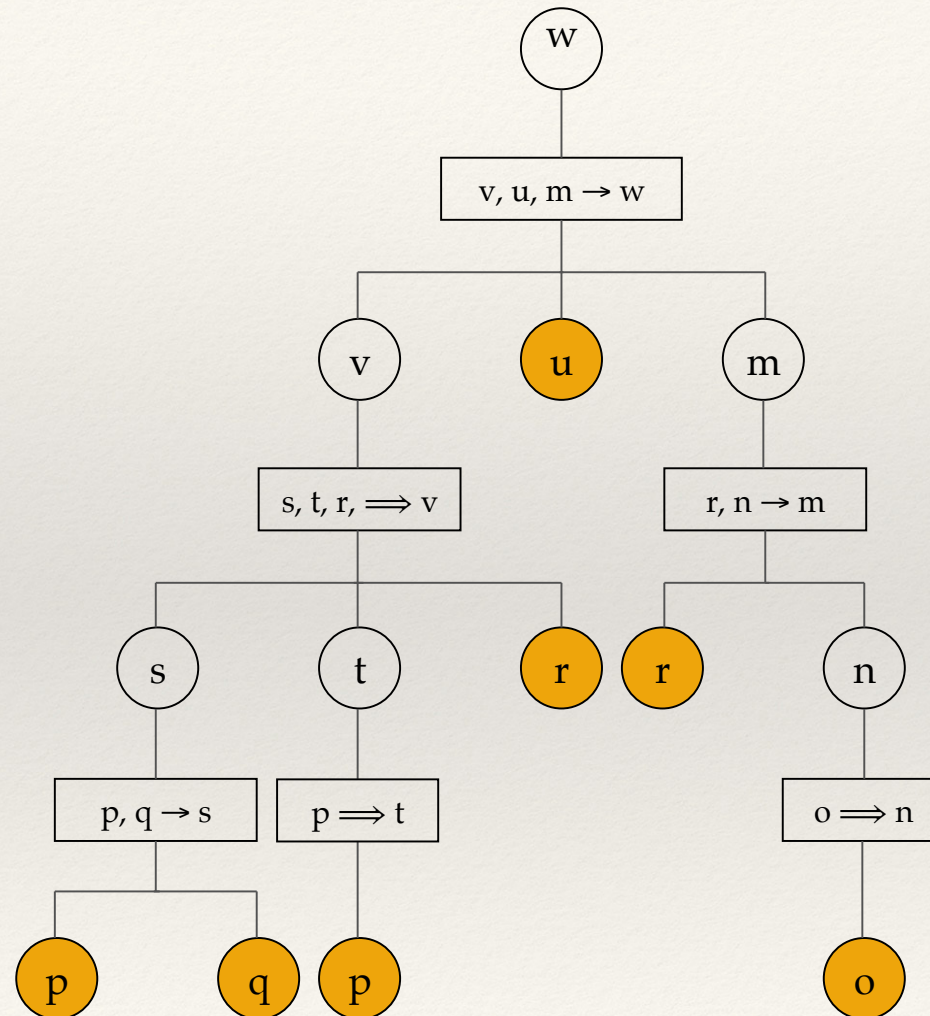
Conclusion





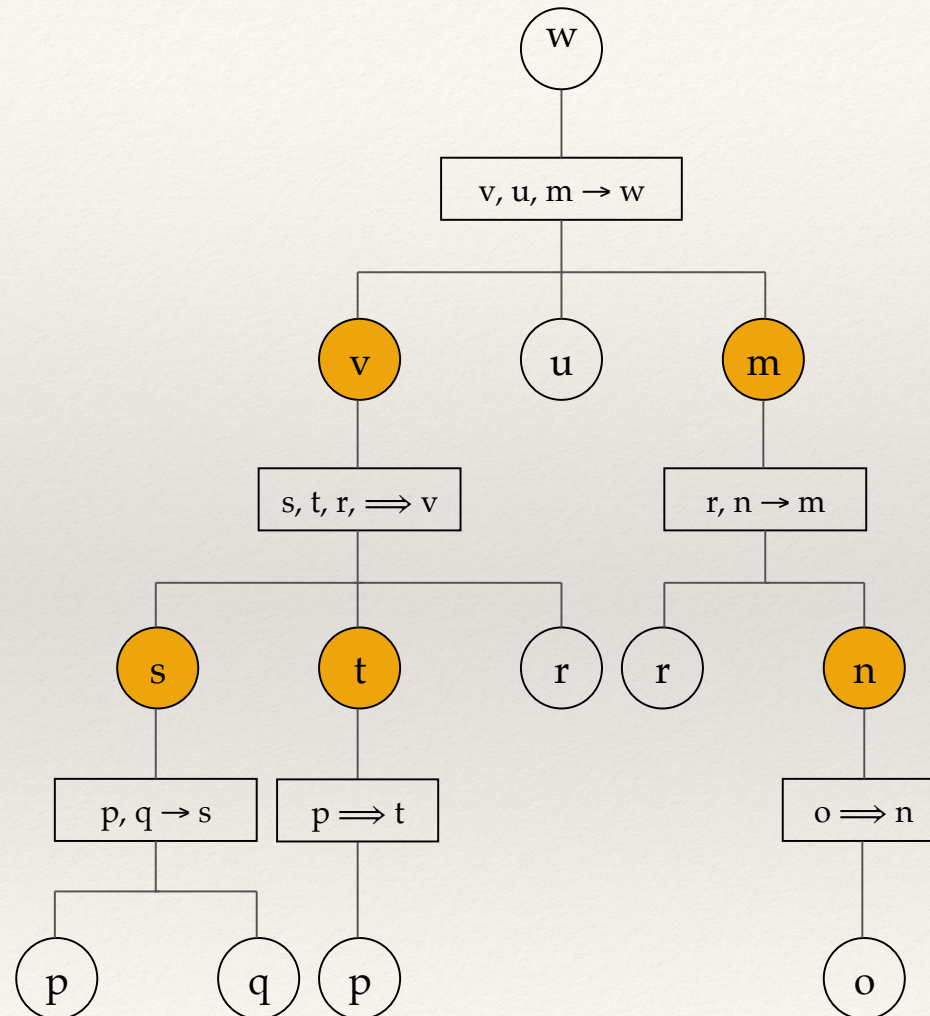
# Structured argumentation based on ASPIC+: Arguments

Premises



# Structured argumentation based on ASPIC+: Arguments

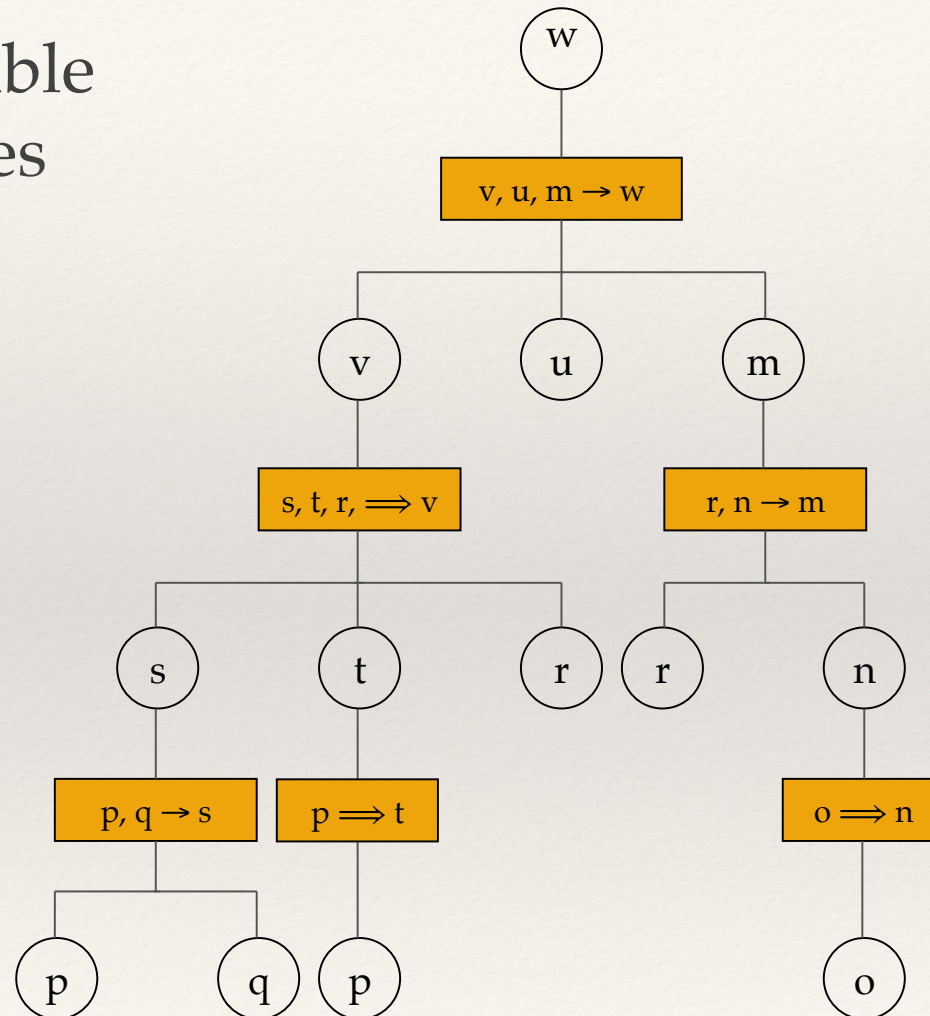
Intermediate  
Conclusions



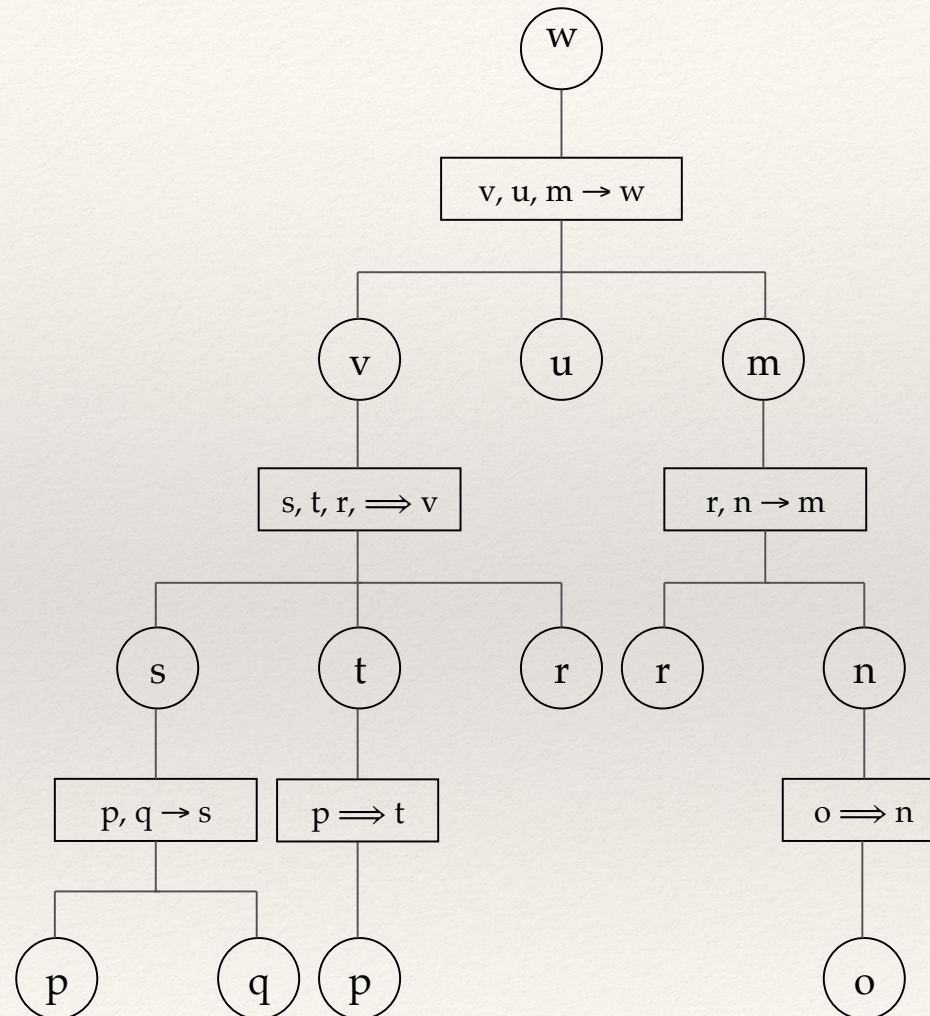


# Structured argumentation based on ASPIC+: Arguments

Strict/Defeasible  
Inference Rules

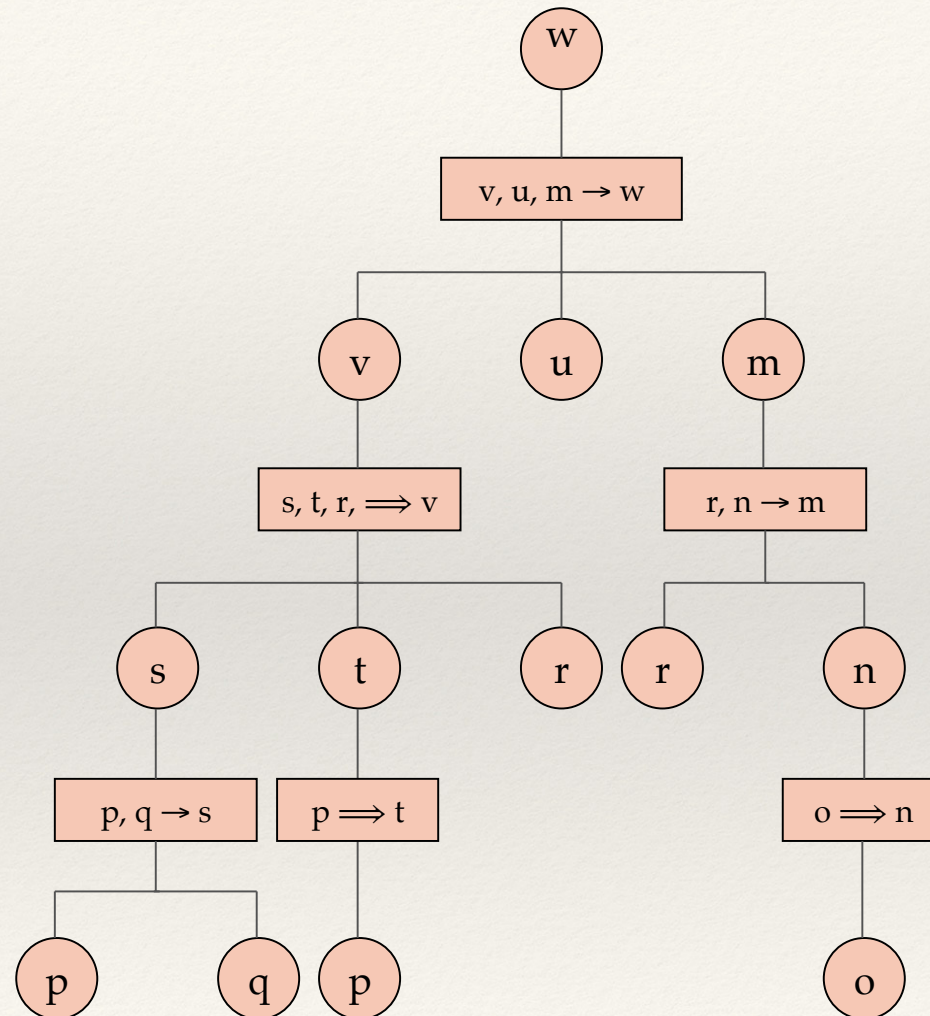


# Belief





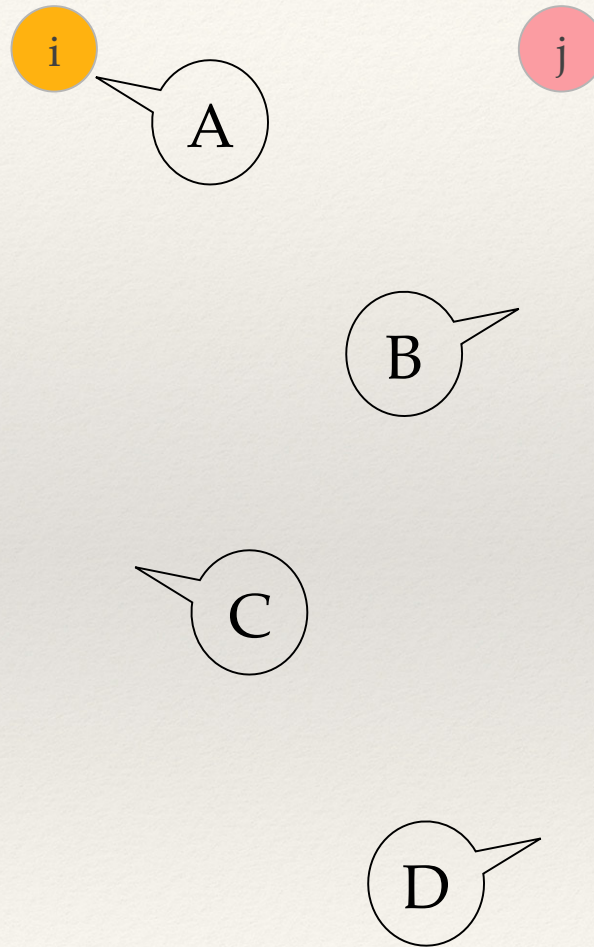
# Belief



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## Opponent modelling using abstract arguments

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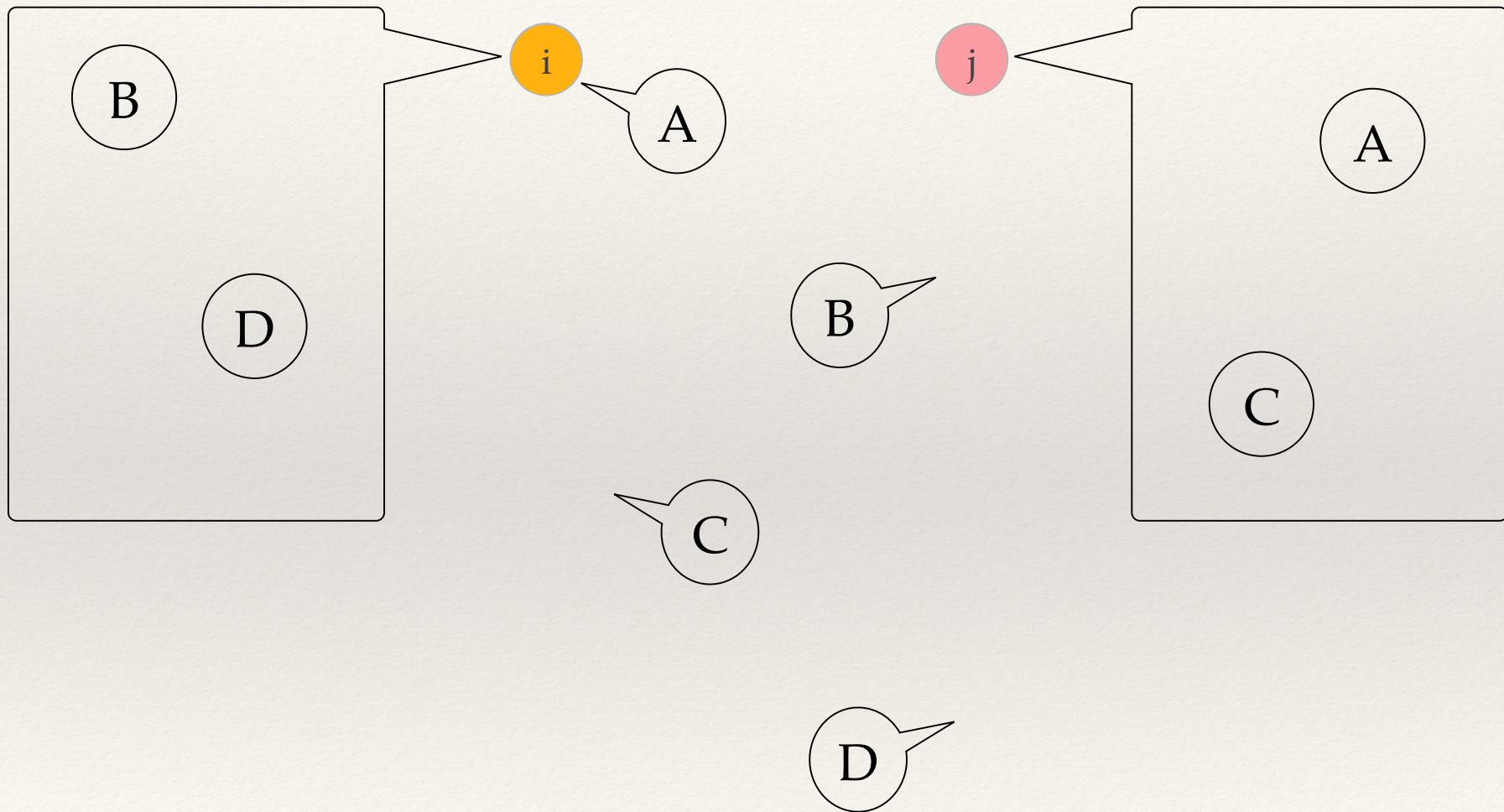




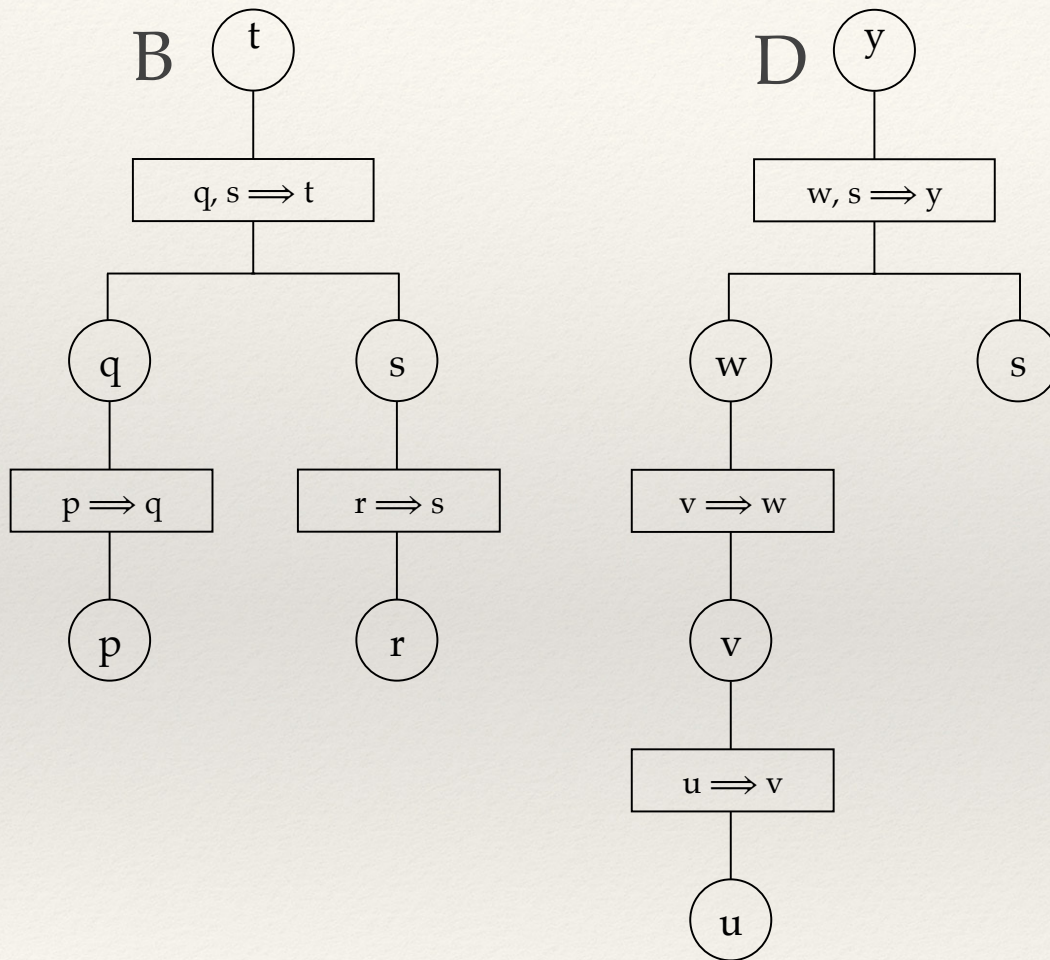
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## Opponent modelling using abstract arguments

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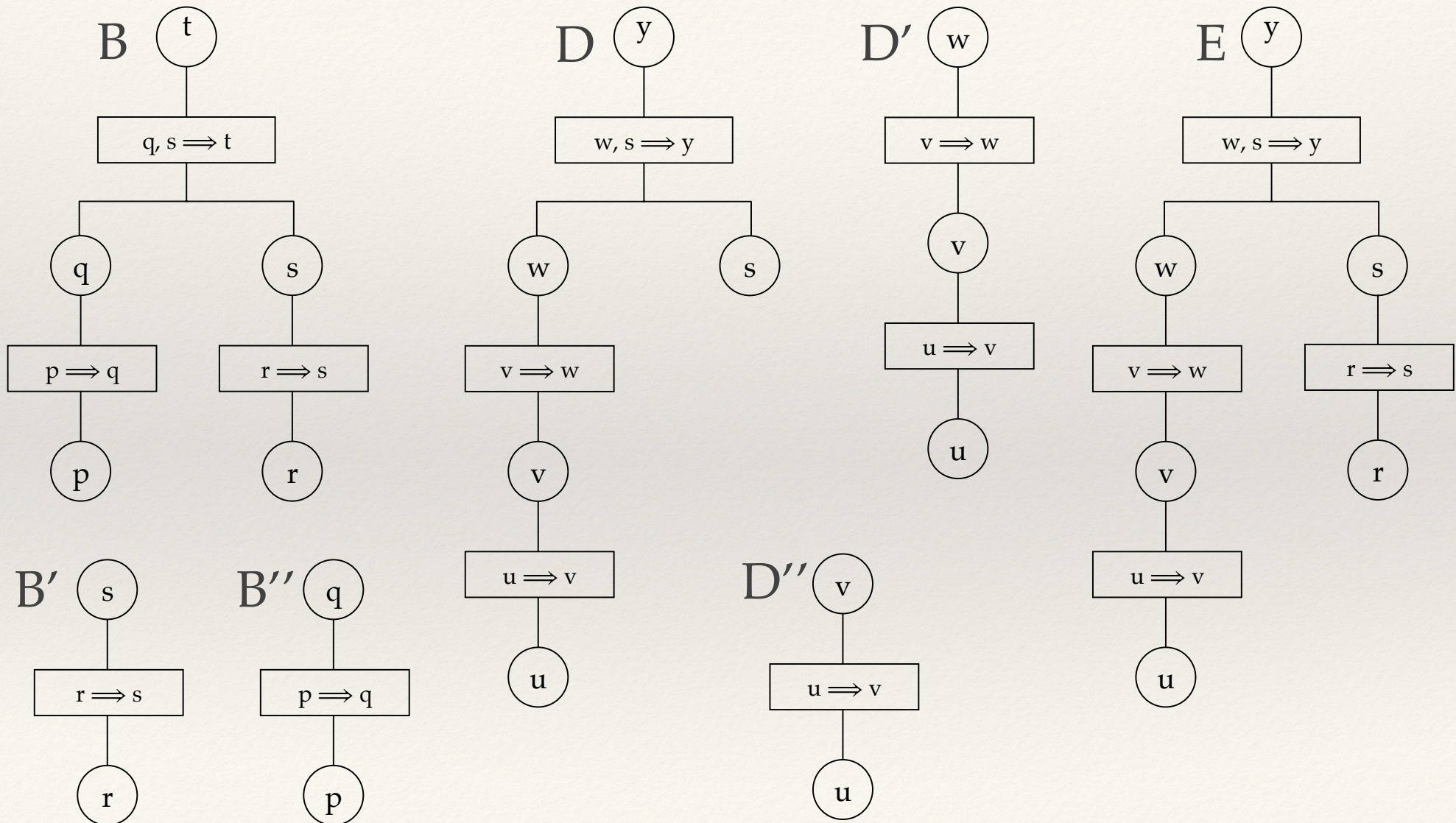


## Opponent modelling: from abstract to structured arguments





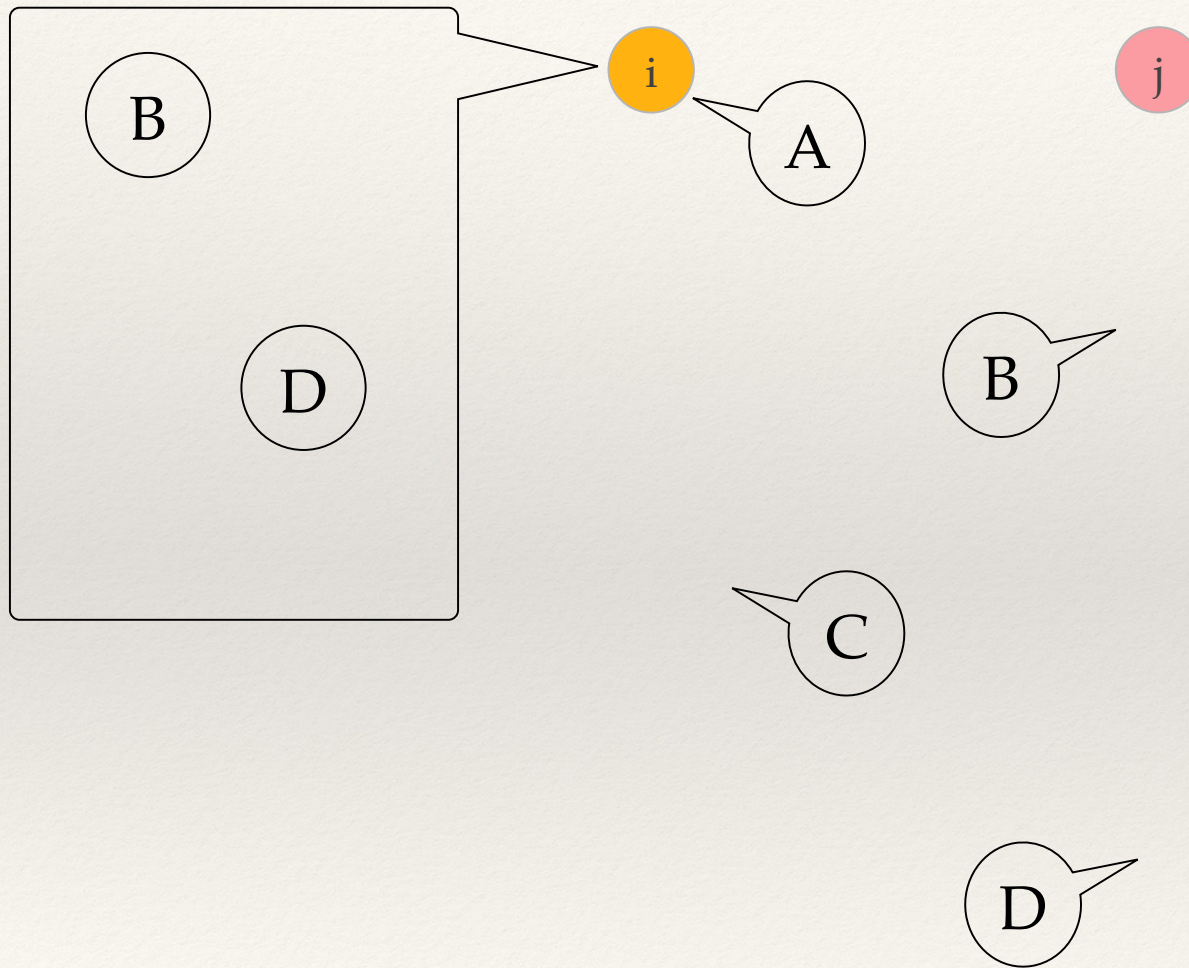
# Opponent modelling: from abstract to structured arguments



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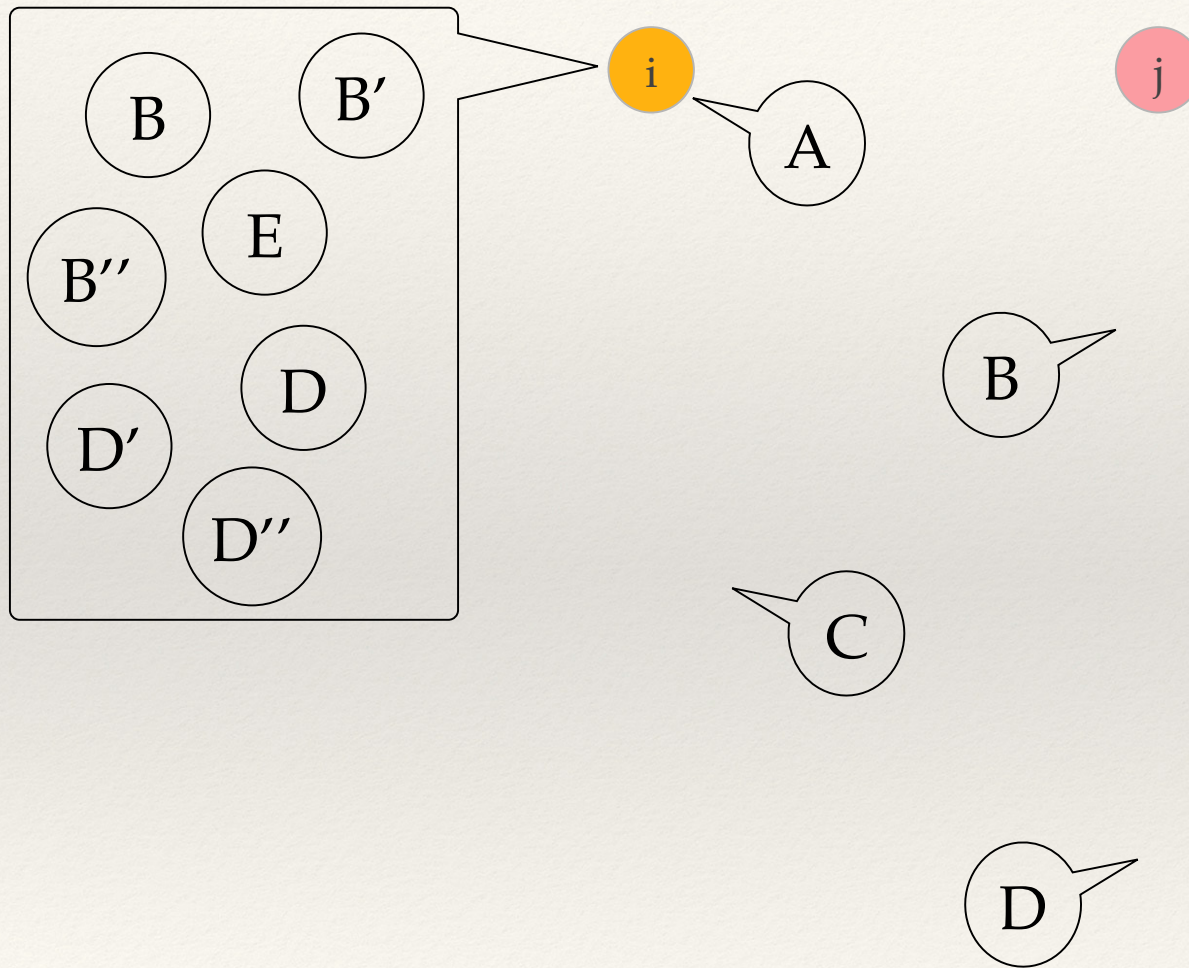




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## Opponent modelling: from abstract to structured arguments

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# Estimating the likelihood of a second-order belief

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**DEF** An agent  $i$ 's second-order belief with regards to agent  $j$  is a belief that agent  $i$  assumes that agent  $j$  has.

We use two complementary methods, the first of which uses

➡ Evidence obtained through dialogue

- ❖ *Example:* agent  $j$  asserts  $\alpha$  in a dialogue with  $i$
- ❖ *Example:* an agent  $k$  informs  $i$  that  $j$  believes in  $\alpha$
- ❖ *Example:* an agent  $i$  finds out that  $j$  does not believe in  $\alpha$  through a failed inquiry dialogue



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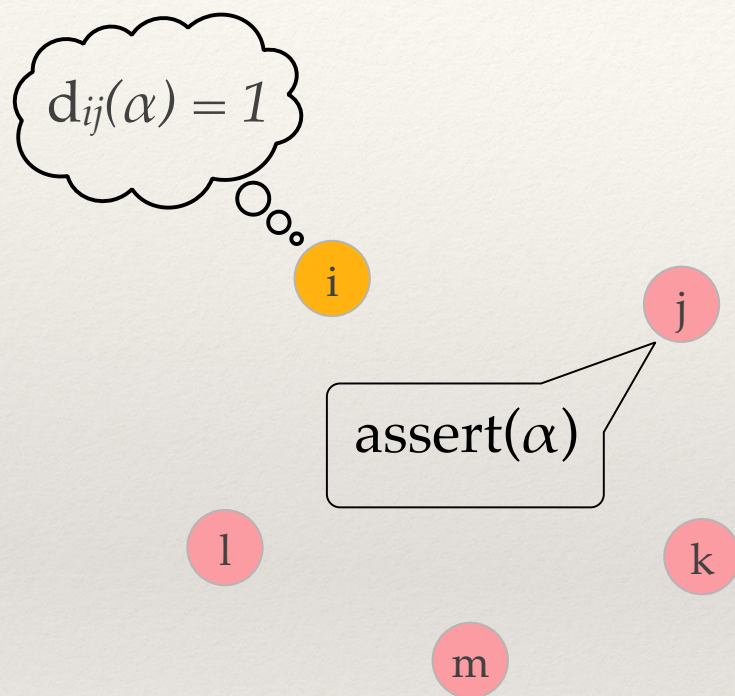
# Dialogical Evidence (DE)

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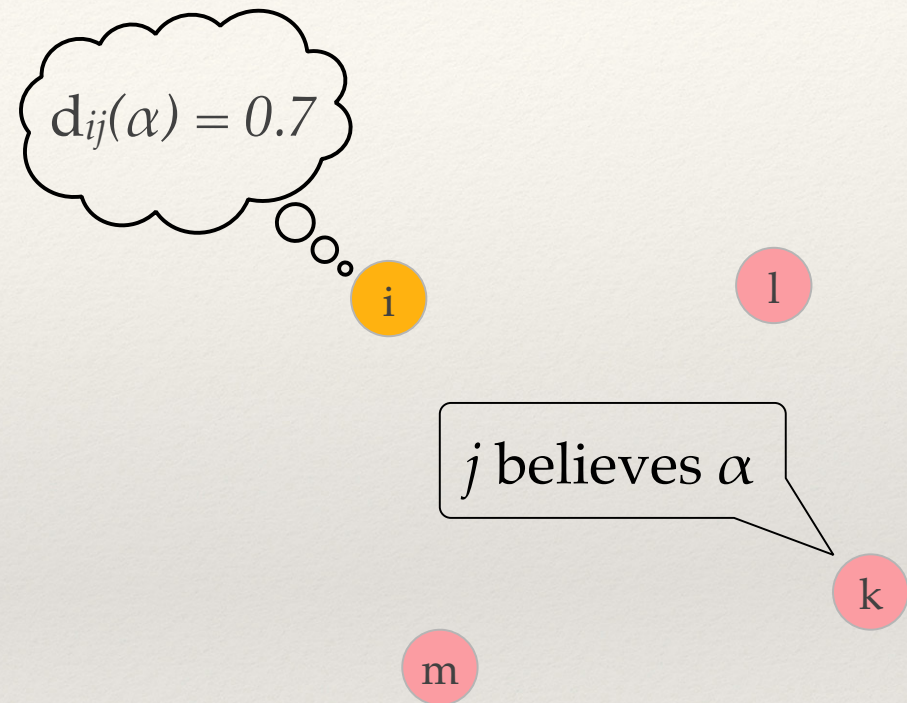
We assume the existence of some mechanism that allows an agent  $i$  to assign the likelihood that  $j$  believes  $\alpha$  based on dialogical interactions. This is denoted by  $d_{ij}(\alpha)$ :

- $d_{ij}(\alpha)=0$  means  $i$  has no information about  $j$ 's believing (or not) in  $\alpha$
- $0 < d_{ij}(\alpha) \leq 1$  means that  $i$  believes that  $j$  believes in  $\alpha$  with degree  $d_{ij}(\alpha)$  of confidence
- $d_{ij}(\alpha) = \perp$  means that  $i$  believes that  $j$  does not believe in  $\alpha$

# Dialogical Evidence (DE)



Direct Evidence



Indirect Evidence



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# Dialogical Evidence (DE) not always available

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# Estimating the likelihood of a second-order belief

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Two complementary methods:

➡ Evidence obtained through dialogue

- ❖ *Example:* agent  $j$  asserts  $\alpha$  in a dialogue with  $i$
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➡ Estimate the likelihood based on the agents' membership to communities



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# Agent Group

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**DEF** A *group* of agents is a set of agents who share certain characteristics.

*Example:* agents with the same goal, history, institutional roles, etc.

*Example:* Lawyers, Logicians, Researchers in the field of argumentation, etc.

Agents may belong to more than one groups.

"Membership to a group licenses the assumption that the member shares some beliefs with the others in the group."

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# Agent Communities

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**DEF** The power set of the set of groups forms the set of all communities: an *agent community* is an element of the set.

So if A and B are groups, the community {A,B} contains the agents that belong to both A and B, and so forth.

If an agent is in community {A,B}:

- *i* has the beliefs shared by the agents in A
- *i* has the beliefs shared by the agents in B
- plus possibly some other beliefs specific to members of both A and B only.

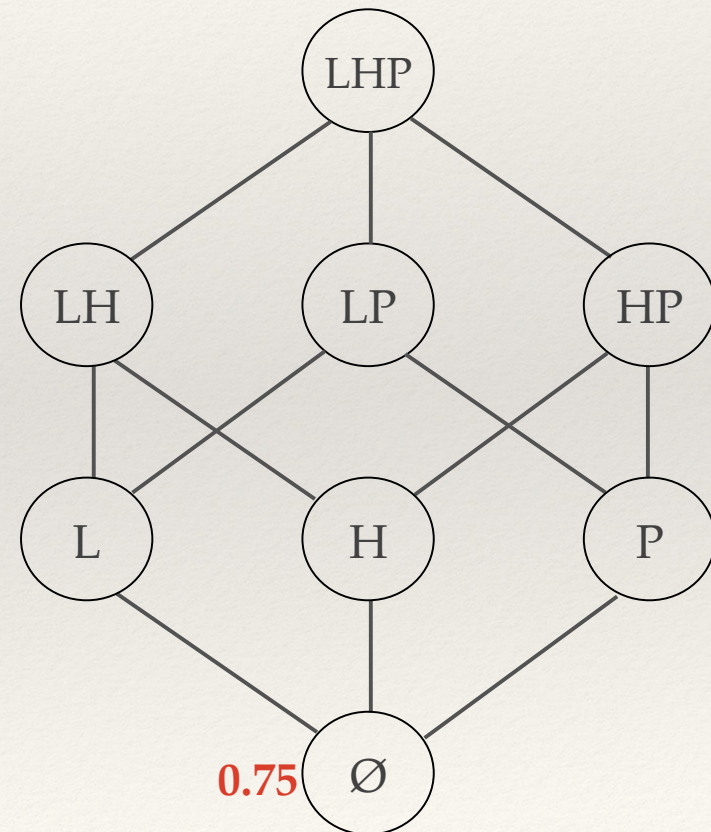
$\emptyset$  is the most general community, to which every agent belongs.



# P-scores

Since an agent knows the communities to which each agent belongs:

- Using the dialogical evidence gathered, an agent assigns to each community  $\kappa$  and belief  $\alpha$ , a *p-score* representing the proportion of agents in that community with positive dialogical evidence.
- Assuming we have 20 agents in total and agent  $i$  knows through dialogical evidence that 15 agents have belief  $\alpha$  and the remaining 5 do not to have the belief  $\alpha$ : the p-score for  $\alpha$  and  $\emptyset$  according to  $i$  will be 0.75

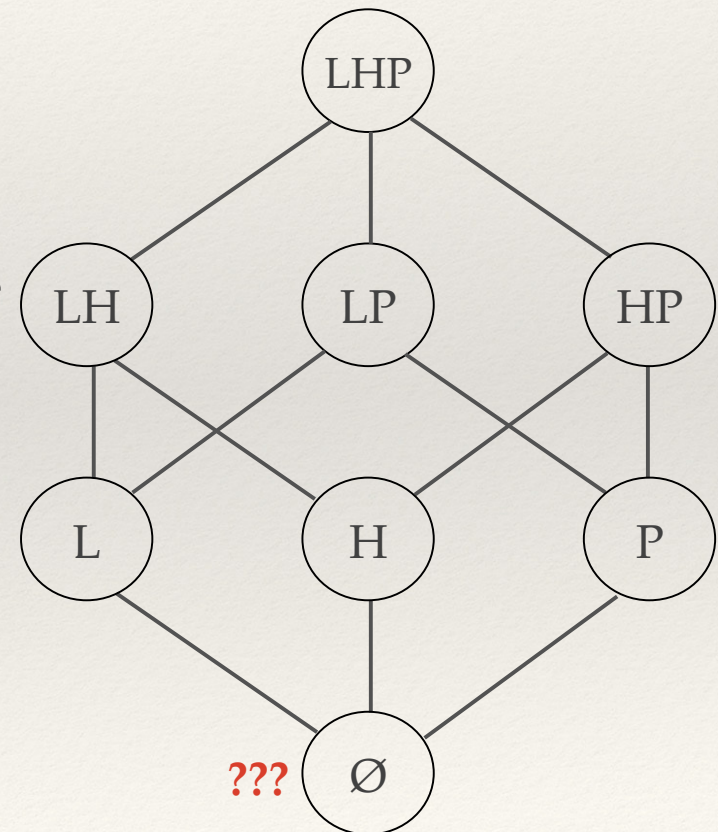




# Refining this notion...

Suppose that out of the 15 agents  $i$  knows to believe  $\alpha$ , 10 actually belong to community L.

- Then in fact, the reason for believing  $\alpha$  could be attributed to the membership to the more specific community.
- This means we then need to remove these agents from  $\emptyset$ 's p-score.
- The systematic way of doing this is to successively remove the agents in a community with maximal p-score from the other more general communities they belong too.

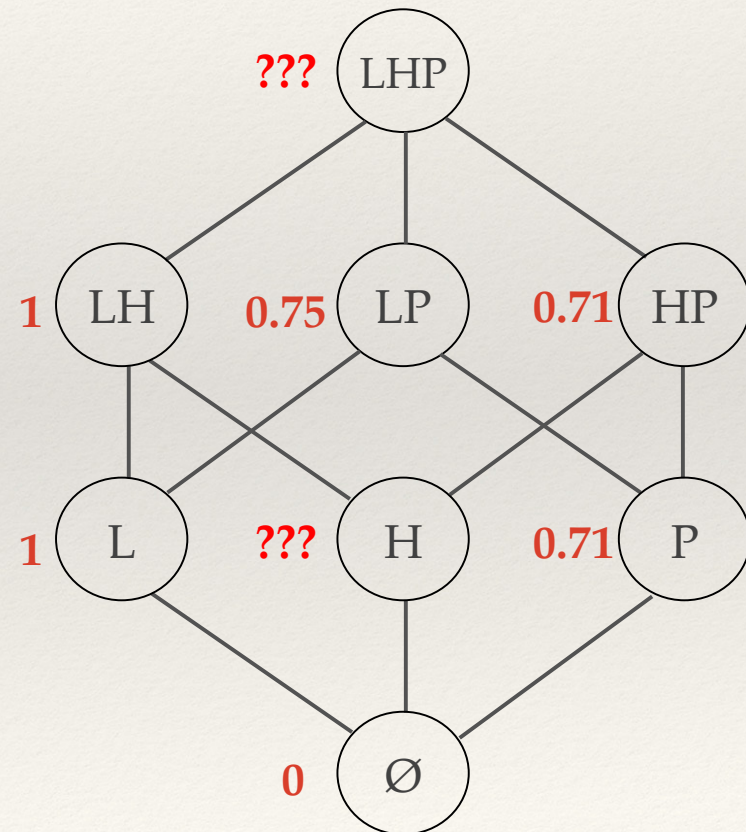




# We need to refine...

This will yield a distribution such as the one on the right, where some values may be missing.

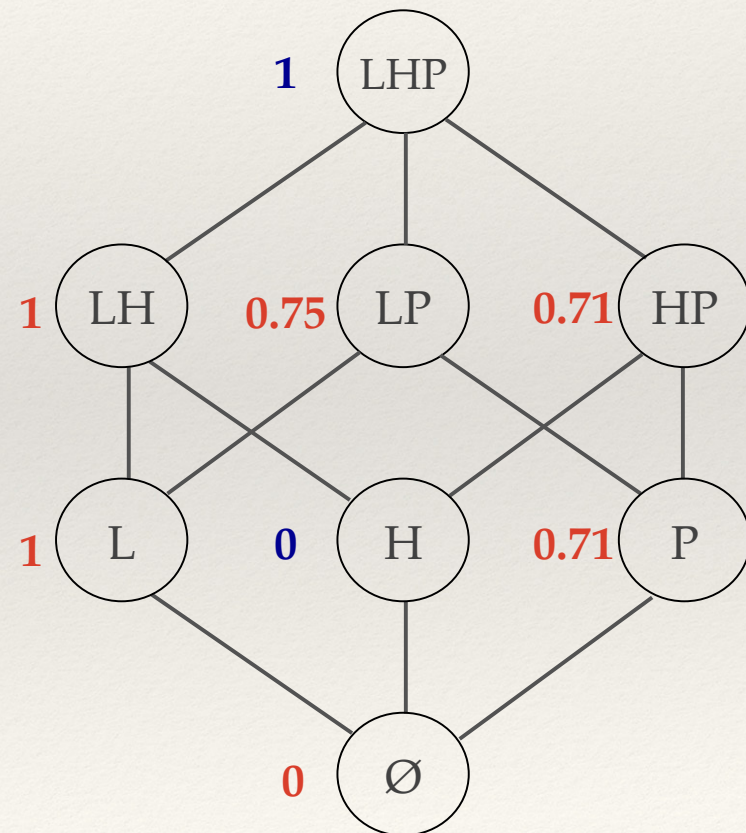
- To complete the assignment, we push the values up, giving each community missing a p-score the maximum of its children.
- So we end up with an assignment  $F(\kappa, \alpha)$  giving the likelihood that a member of the community  $\kappa$  has the belief  $\alpha$ .



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# Community-Based Estimate (CE)

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$c_{ij}(\alpha)$  denotes the likelihood  $i$  assigns to  $j$  believing  $\alpha$  based on  $j$ 's membership in communities using the assignment  $F$  just defined.

**DEF**  $c_{ij}(\alpha) = F(\kappa, \alpha)$ , where  $\kappa$  is the most specific community agent  $j$  belongs to.

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# Combining the Estimates

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**DEF**  $u_{ij}(\alpha)$  denotes the likelihood  $i$  assigns to  $j$  believing  $\alpha$

- If  $d_{ij}(\alpha) > 0$ , then  $u_{ij}(\alpha) = d_{ij}(\alpha)$
- If  $d_{ij}(\alpha) = 0$ , then  $u_{ij}(\alpha) = c_{ij}(\alpha)$
- If  $d_{ij}(\alpha) = \perp$ , then  $u_{ij}(\alpha) = 0$

We can lift this likelihood to arguments via an appropriate function, e.g., min aggregating the values  $u_{ij}(\alpha)$  of the argument's constituent beliefs.



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## Application: Enthymeme Construction

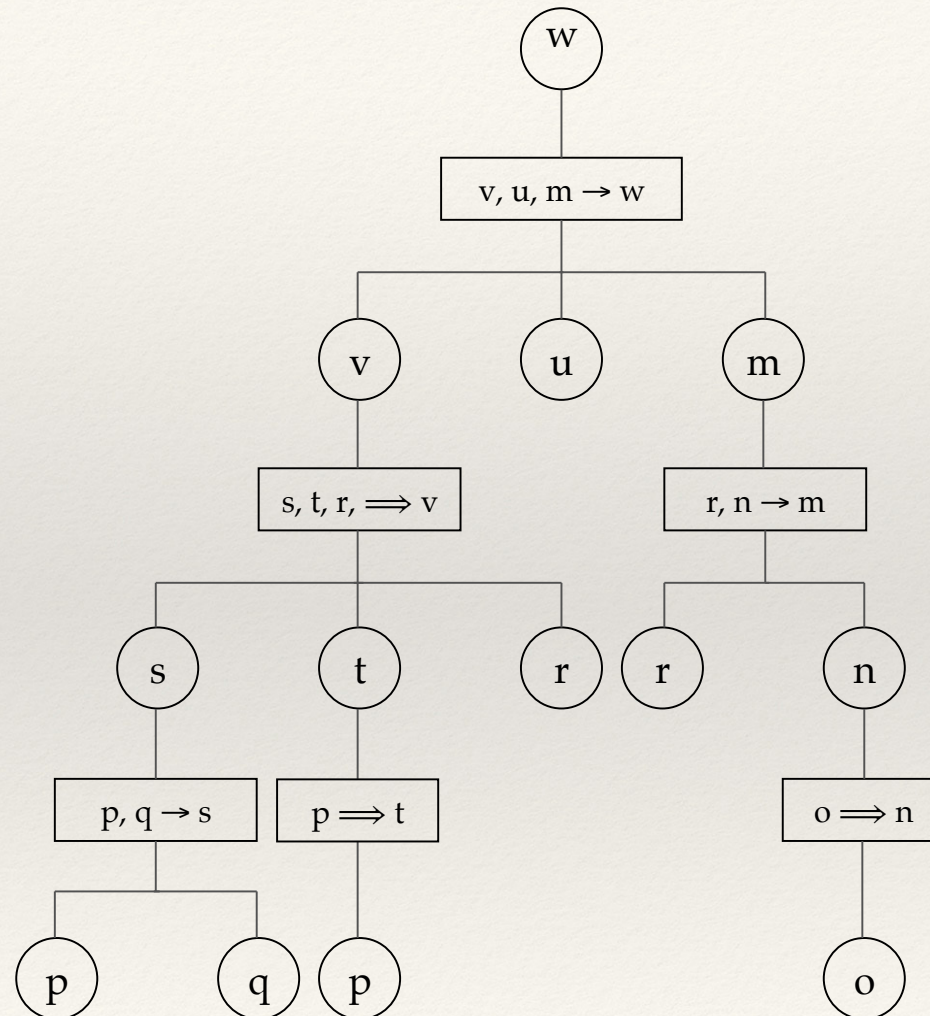
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Sending agent  $i$ :

- ❖ Uses the values  $u_{ij}(\alpha)$  of each belief  $\alpha$  in an argument.
- ❖ Removes nodes exceeding a given threshold  $\tau$
- ❖ Reconnects remaining components using ancestor-descendant relationship in the original argument

# Example

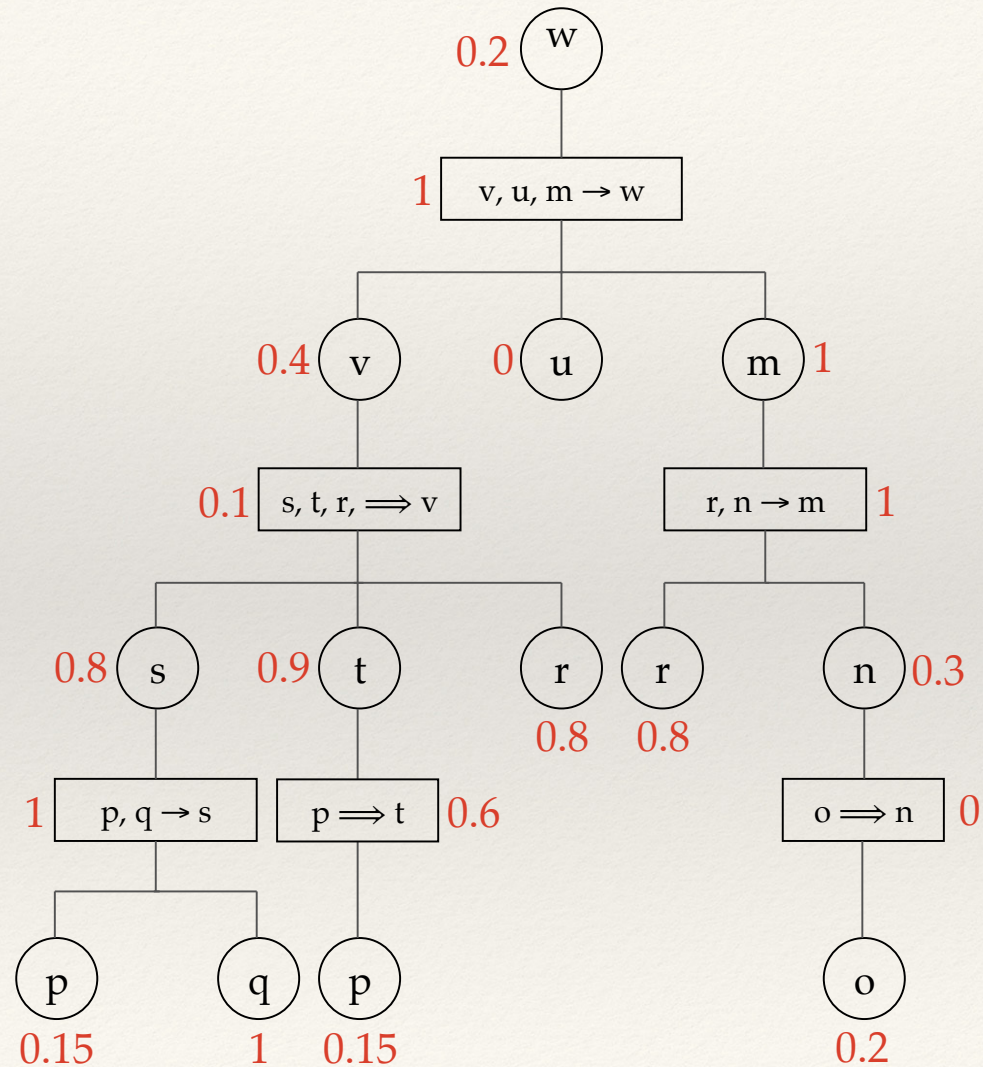
Threshold  $\tau = 0.7$





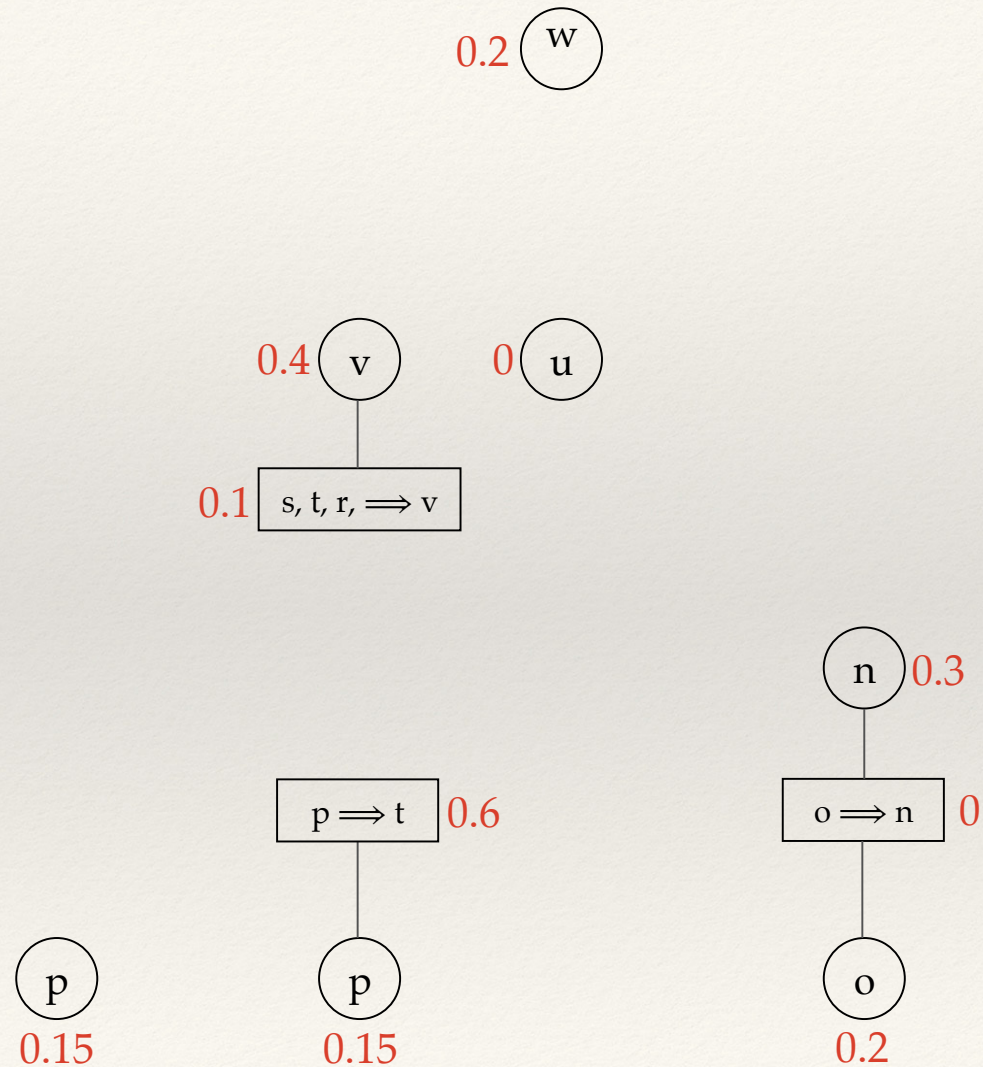
# Example

Threshold  $\tau = 0.7$



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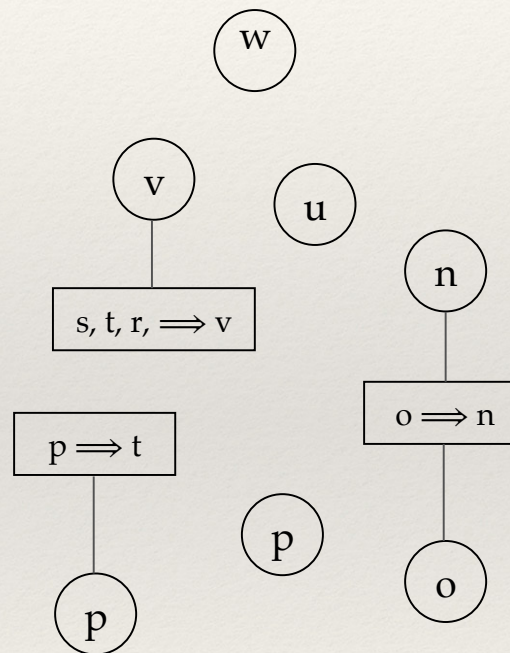


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# Example

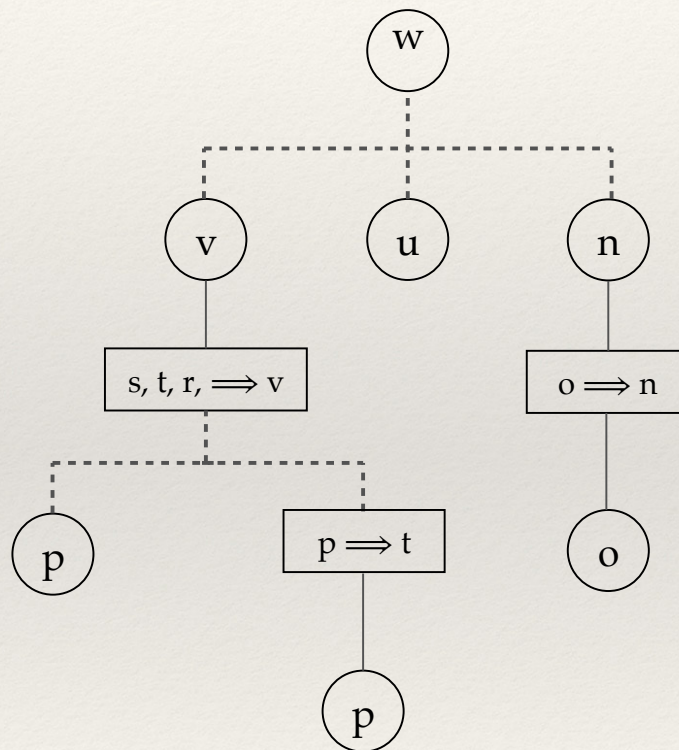
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Threshold  $\tau = 0.7$



# Example

Threshold  $\tau = 0.7$





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# Conclusions and Future work

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- ❖ We allow agents to store the full argument structure.
- ❖ Based on dialogical evidence, we record the likelihood that another agent has certain belief.
- ❖ We also use this information to estimate the likelihood that “similar” agents have some beliefs.
- ❖ Combining these two estimates, we can estimate the likelihood that an agent can construct a certain argument. In the future we would like to estimate the likelihood that an agent considers an argument to be *acceptable*.
- ❖ Our estimates can be made more sophisticated.
- ❖ Conduct some empirical evaluation using human subjects?